

# Al Skills Review

$$\begin{array}{l} \text{Distribute} \\ \textcircled{1} \quad 3(2x-4) = -18 \\ \quad \quad 6x-12 = -18 \end{array} \left. \vphantom{\begin{array}{l} \text{Distribute} \\ \textcircled{1} \quad 3(2x-4) = -18 \\ \quad \quad 6x-12 = -18 \end{array}} \right\} \begin{array}{l} \text{yes... equal.} \\ \text{used the distributive} \\ \text{property } \textcircled{C} \end{array}$$

$$\textcircled{2} \quad \sqrt{16} + \sqrt[3]{8} = 4 + 2 = \boxed{6} \quad \textcircled{B}$$
  
$$\begin{array}{ccc} & \uparrow & \uparrow \\ & \text{b/c} & \text{b/c} \\ & 4 \cdot 4 = 16 & 2 \cdot 2 \cdot 2 = 8 \end{array}$$

$$\textcircled{3} \quad X^6 X^2 = X^{6+2} = \boxed{X^8}$$

A.  $X^4 X^3 = X^{4+3} = X^7$  NO

$\textcircled{B}$   $X^5 X^3 = X^{5+3} = X^8$  YES

C.  $X^7 X^3 = X^{7+3} = X^{10}$  NO

D.  $X^9 X^3 = X^{9+3} = X^{12}$  NO

$\textcircled{4}$  the reciprocal of A is  $\frac{1}{A}$  (so basically you flip the fraction)  
You cannot divide by zero...  $\frac{A}{1}$   
so 0 doesn't have A reciprocal  $\textcircled{B}$

$\textcircled{5}$  multiplicative inverse is the same as the reciprocal (so the flipped version of the fraction)  
so flip  $\frac{1}{2}$  to get  $\frac{2}{1} = \boxed{2}$   $\textcircled{D}$

$\textcircled{6}$   $|2x-3|=5$  means  
either

$2x-3=5$

OR

$2x-3=-5$

$2x=8$

$\boxed{x=4}$

$2x=-2$

$\boxed{x=-1}$

$\textcircled{C}$

$$\textcircled{7} \quad 5 - |x+4| \leq -3$$

$$-5 \quad -5 \text{ SA}$$

Solve down to  
Abs. value w/  
SADMEP  
(PEMDAS backwards)

$$-|x+4| \leq -8 \quad \text{DM}$$

FLIP INEQUALITY  
SIGN WHEN YOU MULT  
OR DIVIDE BY  $\ominus$

$$|x+4| \geq 8 \quad \text{"abs. val greater than"} = \text{OR}$$

$\oplus$  CASE

$\ominus$  CASE

← FLIP INEQUALITY  
SIGN FOR  $\ominus$  CASE

$$x+4 \geq 8 \quad \text{OR} \quad x+4 \leq -8$$

$$x \geq 4 \quad \text{OR} \quad x \leq -12$$

$\textcircled{D}$

$$\textcircled{8} \quad 5x - 2(7x+1) = 14x$$

$$5x - 14x - 2 = 14x$$

$$-9x - 2 = 14x \quad \textcircled{A}$$

$$\textcircled{10} \quad C = 360$$

$$C = 120 + 60n$$

$$360 = 120 + 60n \quad \text{SA}$$

$$-120 \quad -120$$

$$240 = 60n \quad \text{DM}$$

$$60 \quad 60$$

$$4 = n \quad \textcircled{B}$$

$$\textcircled{11} \quad 3(x+5) = 2x+35$$

$$3x+15 = 2x+35$$

$$-2x \quad -2x$$

$$x+15 = 35 \quad \text{*step 2}$$

$$\text{SAYS } 5x+15=35$$

$\textcircled{B}$

$$\textcircled{9} \quad 4(2-5x) = 6-3(1-3x)$$

$$8-20x = 6-3+9x$$

$$8-20x = 3+9x$$

$$+20x \quad +20x$$

$$8 = 3+29x$$

$$-3 \quad -3$$

$$5 = 29x$$

so

$$29x = 5 \quad \textcircled{C}$$

$$\textcircled{12} \quad \begin{array}{ccc} \text{1st piece} & \text{2nd piece} & \text{3rd piece} \\ \downarrow & \downarrow & \downarrow \\ 2x & x & 3x \end{array}$$

twice  
as long as  
2nd  
piece

3 times as  
long as 2nd  
piece

$$\text{TOTAL} = 2x + x + 3x$$

$$= 6x$$

$$120 = 6x$$

$$x = 20$$

$$\text{longest piece} = 3x$$

$$= 3(20) = 60 \quad \textcircled{C}$$

$$250X + 750 \leq 2500$$
cost per hour      hour      Flat rate for day  
 (TOTAL DAILY COST)  
 SA:  $-750$        $-750$

DM: 
$$\frac{250X}{250} \leq \frac{1750}{250}$$

$$X \leq 7$$
 (C)

(14)  $X - 5 > 14$   
 +5    +5    SA

$$X > 19$$
 (B)

(18) (D) Anyone that is in the band is a good musician, thus D is true

(15) Perimeter = sum of sides  
 side 1 + side 2 + side 3 = perimeter  
 $y + y + 1 + 7 = 56$

$2y + 8 = 56$

$2y = 48$

$$y = 24$$
 (A)

(16) you need a number that is divisible by neither 2 nor 3

~~(A)~~ no, 100 is divisible by 2,  $100/2 = 50$

~~(B)~~ no, 57 is divisible by 3,  $57/3 = 19$

~~(C)~~ no, 30 is divisible by both  $\frac{30}{3} = 10$ ,  $\frac{30}{2} = 15$

\* (D) 25 is a  $\oplus$  integer but is not divisible by 2 or 3

(17) the "conclusion" is the statement after "then"  
 so "x = -2 or x = 2" (D)

(19) plug in  $x$  for each value given, see which does NOT yield a prime #

• (A)  $(5)^2 + 5 + 5 = 25 + 10 = 35 \in$  NOT prime

NO need to check ~~A~~ B, C, D  $35 = 5 \cdot 7$  or  $1 \cdot 35$   
not prime

(20) step 2, john set two factors equal to zero. this is the "zero product property" (B)  
IF  $AB = 0$  then  $A = 0$  or  $B = 0$

(21)  $n + 8(n + 20) = 110$

$n + 8n + 160 = 110 \leftarrow$  stan is wrong in step 1 (B)

(22) "the opposite of a number is less than the original number" is only true if the original is positive (thus the opposite is negative and  $\ominus < \oplus$ ) (C)  
You can also test #'s to see that

A. never true

# = 7, opposite = -7

B. Always true

# = 0, opposite = 0  
 $-7 < 7 \checkmark \leftarrow$  true here

$0 < 0$  FALSE here

(C) positives only  $\leftarrow$  yup (see ex. in A.)

D. negatives only  $\leftarrow$  nope

# = -5, opp = 5

$5 < -5$  FALSE

(23)  $4x + 2y = 12$  solve for  $y$  to get  $y = mx + b$   
 $\frac{2y}{2} = \frac{-4x + 12}{2}$  SA DM  $y = \text{int}$

$y = -2x + 6$

Y-INT IS

$6$

(C)

(24) IT'S shaded above, so  $y$  is "greater than"  
(NOT A or B)

• IT'S A SOLID LINE so  $y$  is "equal to"  
(NOT A or C)

SO IT HAS TO BE (D)

$$y \geq \frac{1}{2}x - 1$$

ALL 4 ANS HAVE  
same  $mx+b$

(25)  $y = 2x - 2$

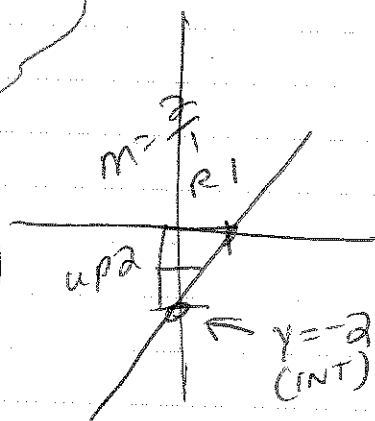
$\uparrow$   $\uparrow$   
y-int @  $y = -2$   
(NOT B or D)

$m = 2 \leftarrow$  rise up 2  
 $T \leftarrow$  run right 1

SO  $\nearrow$  not  $\searrow$   
 $\oplus$  slope  $\ominus$  slope

(NOT C or B)

SO (A)



(26) graph is shaded below ( $y <$  or  $y \leq$ )  
graph is solid line (so "equal to")

y-int is @  $y = 2$

$$\text{slope} = \frac{\text{down } 3}{\text{right } 1} = \frac{-3}{1} = -3$$

$$\boxed{y \leq -3x + 2} \leftarrow \text{see which ANS matches}$$

$$+3x \quad +3x$$

$$\boxed{3x + y \leq 2} \quad (A)$$

(27) line has y-int @  $y=0$  (the origin)

line has slope  $m = \frac{\text{2 up}}{\text{1 right}} = \frac{2}{1}$

$$y = 2x + 0 \quad (B)$$

(28)  $3x + 6y = 2$  just plug in to see which gives true statement

~~(A)~~  $(0, 2)$

$$3(0) + 6(2) = 2$$

$$12 = 2$$

NO

~~(B)~~  $(0, 6)$

$$3(0) + 6(6) = 2$$

$$36 = 2$$

NO

★

(C)  $3(1) + 6(-\frac{1}{6}) = 2$

$$3 + -1 = 2$$

$$2 = 2$$

yes

(29) point-slope is best here

$$y - y_1 = m(x - x_1)$$

$$y - (-10) = 4(x - 3)$$

$$y + 10 = 4x - 12$$

$$\boxed{y = 4x - 22}$$

OR slope-int

$$y = 4x + b$$

$$-10 = 4(3) + b$$

$$-10 = 12 + b$$

$$-12 - 12$$

$$-22 = b$$

(C)

$$\boxed{y = 4x - 22}$$

(A)

c is the "y" and h is the "x"

$$(30) m = \frac{\Delta c}{\Delta h} = \frac{30 - 15}{5 - 2} = \frac{15}{3} = 5$$

point-slope

$$c - c_1 = m(h - h_1)$$

$$c - 15 = 5(h - 2)$$

$$c - 15 = 5h - 10$$

$$\boxed{c = 5h + 5}$$

or  $c = mh + b$

$$c = 5h + b$$

$$15 = 5(2) + b$$

$$15 = b$$

$$\overset{-10}{-10} \quad 5 = b$$

$$\boxed{c = 5h + 5}$$

(C)

(31)  $m = \frac{\Delta y}{\Delta x} = \frac{7-1}{3-1} = \frac{6}{2} = 3$  ← so it's (C)  
 (the only EQ with  $m=3$ )

you CAN finish it  
 (but why?)

$y = 3x - 2$

$y - y_1 = m(x - x_1)$

$y - 1 = 3(x - 1)$

$y - 1 = 3x - 3$

$y = 3x - 2$

(33) parallel means same slope

$y = \frac{5}{4}x + 2$

$m = \frac{5}{4}$

so (A)

(only one w/ slope =  $\frac{5}{4}$ )

PUT BOTH in slope-int  
 line l line q

$6x + 5y = 3$

$5x - 6y = 0$

$5y = -6x + 3$

$-6y = -5x$

$y = -\frac{6}{5}x + \frac{3}{5}$

$y = \frac{5}{6}x$

$m = -\frac{6}{5}$

$m = \frac{5}{6}$

$b = \frac{3}{5} \leftarrow \text{NOT } b = 0$

(A) NO, one is  $\frac{3}{5}$ , other is 0

(B) no, slopes are not equal

(C) no, plug in  $y=0$

$6x + 0 = 3$

$5x = 0$

$x = \frac{1}{2}$

$x = 0$

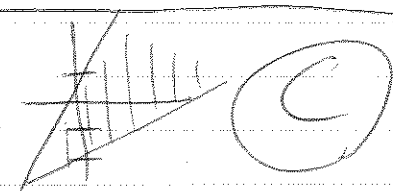
← not the same

(D) Yes! slopes are opposite reciprocals

(34) ①  $2x \geq y - 1$

②  $2x - 5y \leq 10$

↑ symbol is missing in PDF so I wrote it in



①  $-y \geq -2x - 1$

②  $-5y \leq -2x + 10$

$y \leq 2x + 1$   
 (below, solid line)

$y \geq \frac{2}{5}x - 2$   
 (solid line shade above)

$$(35) \begin{cases} y = -3x - 2 \\ 6x + 2y = -4 \end{cases}$$

substitution

$$6x + 2(-3x - 2) = -4$$

$$6x - 6x - 4 = -4$$

$$-4 = -4 \leftarrow$$

all variables  
cancel to  
leave  
true statement  
SO INFINITE  
SOLNS

(D)

$$(36) \begin{cases} x + 3y = 7 \\ (x + 2y = 10)(-1) \end{cases} \rightarrow \begin{array}{r} x + 3y = 7 \\ -x - 2y = -10 \\ \hline \end{array}$$

$$y = -3$$

has to be (D)

but if you want to finish...

plug  $y = -3$  into either EQ

$$x + 3(-3) = 7$$

$$x - 9 = 7$$

$$\boxed{x = 16}$$

$$\rightarrow (16, -3)$$

$$(-, -3)$$

$$(37) \begin{cases} d = \text{dimes}, q = \text{quarters} \\ (d + q = 100)(-10) \end{cases} \rightarrow$$

$$.10d + .25q = 14.05$$

use elimination

$$-.10d - .10q = -10$$

$$.10d + .25q = 14.05$$

$$.15q = 4.05$$

$$q = \frac{4.05}{.15} = 27$$

(A)



$$(38) \quad y = -2x + 3 \quad \leftarrow \text{SAME (identical) line} \downarrow$$

$$\frac{5y}{5} = \frac{-10x + 15}{5 \cdot 5} \rightarrow y = -2x + 3$$

(A)

$$(39) \quad \frac{5x^3}{10x^7} = \frac{\cancel{5} \cdot \cancel{x} \cdot \cancel{x} \cdot x}{\cancel{5} \cdot 2 \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x} \cdot x \cdot x \cdot x \cdot x}$$
$$= \frac{1}{2 \cdot x \cdot x \cdot x \cdot x} = \boxed{\frac{1}{2x^4}} \quad (B)$$

$$(40) \quad (4x^2 - 2x + 8) - (x^2 + 3x - 2)$$

$$= 4x^2 - 2x + 8 - x^2 - 3x + 2$$

$$= 3x^2 - 5x + 10 \quad (D)$$

(41) let  $P(x)$  be the "mystery polynomial"

$$3x^2 - 2x + P(x) = 5x^2 - 6x \quad \text{solve for } P(x)$$
$$-3x^2 + 2x \quad \quad -3x^2 + 2x$$

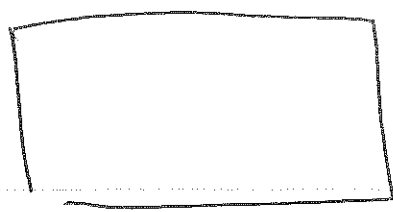
$$\boxed{P(x) = 2x^2 - 4x} \quad (A)$$

$$(42) \quad (x+2) + (x-2)(2x+1)$$

$$x+2 + \begin{matrix} \text{FOIL} \\ F + O + I + L \\ 2x^2 + x - 4x - 2 \end{matrix}$$

$$= 2x^2 + (-2x) + 0 = \boxed{2x^2 - 2x} \quad (A)$$

43



length = 2x

(not drawn to scale)

width = x

$$A = L \cdot W = 2x \cdot x = 2x^2$$

(B)

44

$$3a^2 - 24ab + 48b^2 \leftarrow \text{gcf of 3...}$$

SO ANS IS C or D

$$3(a^2 - 8ab + 16b^2)$$

↑  
front seats  
a · a

↑  
same sign

sign is ⊖

back seats need to multiply to 16b<sup>2</sup> so

- 4b · 4b
- 2b · 8b
- 1b · 16b

$$= 3(a - 4b)(a - 4b)$$

(C)

OR FOIL out all ANS, see which is right

45

$$x^2 - 11x + 24$$

↑  
x · x  
front seats

↑  
same sign

sign is ⊖

- back seats
- 1, 24
  - 2, 12
  - 3, 8
  - 4, 6

$$= (x - 3)(x - 8)$$

(B)

check by FOILING

$$x^2 - 3x - 8x + 24$$

$$x^2 - 11x + 24 \checkmark$$

46

$$9T^2 + 12T + 4$$

3T · 3T  
1T · 9T

↑  
same sign

sign is ⊕

$$= (3T + 2)(3T + 2)$$

FOIL to check

$$9T^2 + 6T + 6T + 4$$

$$= 9T^2 + 12T + 4 \checkmark$$

ALWAYS GUESS middle #'s (closer together first)

$$\text{ANS: } (3T + 2)^2$$

(A)

$$(47) 32 - 8z^2$$

$$-8(z^2 - 4) \leftarrow \textcircled{1} \text{ take out gcf}$$

$\leftarrow \textcircled{2}$  binomial is difference of (D.O.S) squares

$$\boxed{8(z+2)(z-2)}$$

$$A^2 - B^2 = (A+B)(A-B)$$

ANS... but not listed... so they must have only taken out 8 as gcf

$$32 - 8z^2 = 8(4 - z^2) = \underbrace{8}_{\text{D.O.S}} \underbrace{(2+z)(2-z)}_{\textcircled{B}}$$

$$(48) x^2 + x = 42$$

solve for x by making one side = 0 then factoring

$$x^2 + x - 42 = 0$$

$\uparrow$   
x-x

opposite signs  
6, 7  
3, 14  
2, 21  
1, 42

solve  
 $x + 7 = 0$

$$x = -7$$

$$x - 6 = 0$$

$$x = 6$$

$$(x+7)(x-6) = 0$$

$\star \textcircled{A}$

FOIL to check

$$x^2 + 7x - 6x - 42$$

$$x^2 + x - 42 \checkmark$$

OR

plug in ANS to see which yields 42

$$\textcircled{A} (-7)^2 + (-7) = 49 - 7 = 42 \checkmark$$

$$B. (-6)^2 + -6 = 36 - 6 = 30 \text{ NO}$$

$$C. (14)^2 + 14 = 196 + 14 = 210 \text{ NO}$$

$$D. (42)^2 + 42 = \underline{\text{WAY TO BIG}} \text{ NO}$$

$$(49) x^2 - 8x = 5$$

$$\bullet 1(x^2 - 8x + 16) = 5 + 16$$

$$\begin{array}{l} \div 2 \downarrow \\ (-4) \swarrow \text{sq} \end{array}$$

$$\begin{array}{l} \uparrow \\ \text{ADD} \\ 16 \end{array}$$

TO both sides

(C)

$$(50) x^2 + 6x = 16$$

$$x^2 + 6x - 16 = 0$$

x-x

opp signs

$$\begin{array}{l} 1 \cdot 16 \\ 4 \cdot 4 \\ (2-8) \end{array}$$

look at ANS -- it's this

$$\bullet (x+8)(x-2) = 0 \leftarrow \text{FOIL to check}$$
$$x^2 + 8x - 2x - 16$$
$$x^2 + 6x - 16 \checkmark$$

$$x+8=0$$

$$x-2=0$$

$$\boxed{x=-8}$$

$$\boxed{x=2}$$

(C)

$$(51) x^2 + 4x = 6$$

$$1(x^2 + 4x + 4) = 6 + 4$$

$$\begin{array}{l} \div 2 \downarrow \\ (+2) \swarrow \text{sq} \end{array}$$

$$(x^2 + 4x + 4) = 10$$

$$(x+2)^2 = 10 \quad (B)$$

52  $10x^2 - 25x + 15 = 0$

gcf  
5  $(2x^2 - 5x + 3) = 0$

$2x \cdot x$        $\uparrow 1 \cdot 3$   
 same sign  
 sign is  $\ominus$  ← SO NOT A or C

$5(2x - 3)(x - 1)$       check by FOIL

F   O   I   L  
 $2x^2 - 2x - 3x + 3$   
 $2x^2 - 5x + 3 \checkmark$

(D)

53  $x^2 + \frac{b}{a}x + \frac{(b/2a)^2}{a} = \frac{-c}{a} + \frac{(b/2a)^2}{a}$  (D)

$\div 2 \downarrow$        $\uparrow$  SQ  
 $\frac{b}{2a}$

54  $ax^2 + bx + c = 0$   
 $x^2 + \frac{b}{a}x + \frac{c}{a} = 0$

(I)  $x^2 + \frac{b}{a}x = -\frac{c}{a}$

SO III HAS TO BE LAST...  
 order is  
 I, IV, II, III

(IV)  $x^2 + \frac{b}{a}x + \frac{(b/2a)^2}{a} = \frac{-c}{a} + \frac{(b/2a)^2}{a}$  (A)

$\div 2 \downarrow$        $\uparrow$  SQ  
 $\frac{b}{2a}$

$(x + \frac{b}{2a})^2 = \frac{-c}{a} + \frac{b^2}{4a^2}$   
 get common denom of  $4a^2$

(II)  $(x + \frac{b}{2a})^2 = \frac{b^2 - 4ac}{4a^2}$

(55) For  $ax^2+bx+c=0$ ; solns are

$$x = \frac{-b \pm \sqrt{b^2-4ac}}{2a} \quad (\text{the quadratic formula})$$

$$2x^2 - x - 4 = 0$$

$$A=2, B=-1, C=-4$$

$$x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(2)(-4)}}{2(2)} = \frac{1 \pm \sqrt{1+32}}{4}$$

$$x = \frac{1 \pm \sqrt{33}}{4}$$

$$\rightarrow x = \frac{1 + \sqrt{33}}{4} \quad (C)$$

$$\rightarrow x = \frac{1 - \sqrt{33}}{4}$$

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(56)  $x = \frac{-b \pm \sqrt{b^2-4ac}}{2a}$  ← " $b^2-4ac$ " is the discriminant

$$2x^2 + x + 7 = 0$$

$$A=2, B=1, C=7$$

$$b^2-4ac$$

$$1^2 - 4(2)(7)$$

$$1 - 56$$

$$-55 < 0$$

(C)

IF  $b^2-4ac > 0$  then two real solns

IF  $b^2-4ac = 0$  then one real soln

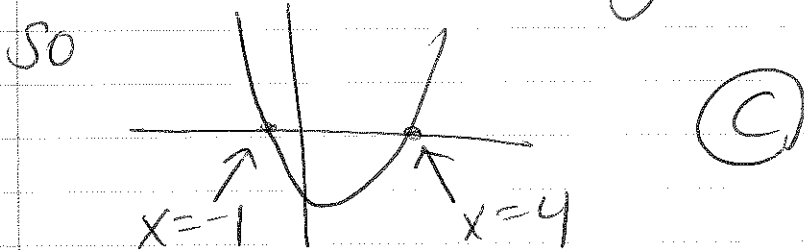
IF  $b^2-4ac < 0$ , then no real soln

57)  $8x^2 + 2x + 1 = 0$   
 $A=8, B=2, C=1$

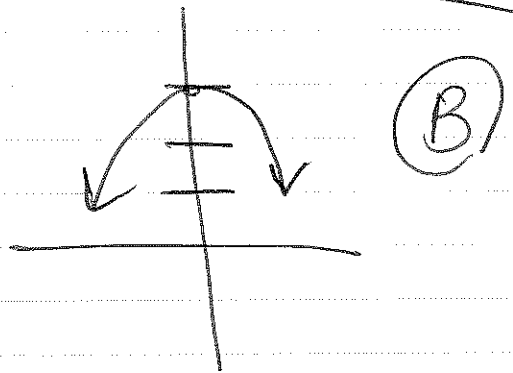
$$x = \frac{-2 \pm \sqrt{2^2 - 4(8)(1)}}{2(8)} = \frac{-2 \pm \sqrt{-28}}{16}$$

(D) no real sol'n

58)  $y=0$  means the x-intercepts (so the x-values where the graph hits the x-axis)



59)  $y = -x^2 + 3$   
 ↑ frown      ↑ w/ y-int at (0, 3)



60) X-INT:  $x=4$  and  $x=-3$

means factors are

$x-(4)$  and  $x-(-3)$

$y = A(x-4)(x+3)$  ← since this isn't a choice, look at ANS

possible gcf (B)  $y = (x+3)$  (2x) gcf of 2

$= 2(x+3)(x-4)$

(61)  $y = 2x^2 - 2x + 3$

how many x-intercepts is asking how many real solns to

$0 = 2x^2 - 2x + 3$

so use DISCRIMINANT ( $B^2 - 4AC$ ) since you only want how many (not the actual solutions)

$A = 2, B = -2, C = 3$

$B^2 - 4AC = (-2)^2 - 4(2)(3) = 4 - 24 = -20 < 0$

NO REAL SOLNS (A)

(62)  $S = vt + 16t^2$

given  $V = 10$   
FIND  $t$  that makes  $S = 84$

$84 = 10t + 16t^2$

$0 = 16t^2 + 10t - 84$

$0 = 2(8t^2 + 5t - 42)$

$0 = 2(t - 2)(8t + 21)$

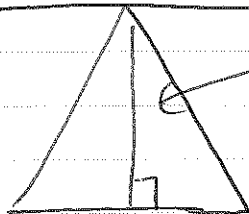
$2 = 0$   
ie  $t = 2$

~~$t = -21/8$~~   
not logical for a time

(A)

← or use  
 $A = 16, B = 10, C = -84$   
 $X = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$

(63)



$h = 2x + 4$   
(4 inches greater than twice the base)

$x = \text{base}$

$(x + 14)(x - 12) = 0$

$x = -14$   
not logical

$x = 12$  (C)

$A = \frac{1}{2}bh = \frac{1}{2}(x)(2x + 4)$

$A = x^2 + 2x$

$168 = x^2 + 2x$

$0 = x^2 + 2x - 168$   
14-12



$$(64) \frac{x^2 - 4xy + 4y^2}{3xy - 6y^2} = \frac{(x-2y)(x-2y)}{3y(x-2y)}$$

$$= \boxed{\frac{x-2y}{3y}} \quad (B)$$

gcf  
 $2x \cdot x$   
 sign same  
 sign  
 1.3

$$(65) \frac{6x^2 + 21x + 9}{4x^2 - 1} = \frac{3(2x^2 + 7x + 3)}{(2x+1)(2x-1)}$$

$$= \frac{3(2x+1)(x+3)}{(2x+1)(2x-1)} = \boxed{\frac{3(x+3)}{2x-1}} \quad (B)$$

$$(66) \frac{x^2 - 4x + 4}{x^2 - 3x + 2} = \frac{(x-2)(x-2)}{(x-1)(x-2)} = \boxed{\frac{x-2}{x-1}} \quad (A)$$

$$(67) \frac{12a^3 - 20a^2}{16a^2 + 8a} = \frac{4a^2(3a-5)}{8a(2a+1)}$$

$$= \frac{\cancel{2} \cdot \cancel{2} \cdot \cancel{a} \cdot \cancel{a} (3a-5)}{\cancel{2} \cdot \cancel{2} \cdot \cancel{a} (2a+1)} = \boxed{\frac{a(3a-5)}{2(2a+1)}} \quad (D)$$

$$(68) \frac{7z^2 + 7z}{4z + 8} \cdot \frac{z^2 - 4}{z^3 + 2z^2 + z} =$$

FACTOR ALL FOUR POLYNOMIALS

GCF  $7z(z+1)$  DIFF. OF SQS  $(z+2)(z-2)$

GCF  $4(z+2)$  GCF  $z(z^2 + 2z + 1)$

keep factoring  $\leftarrow z^2 + 2z + 1 = (z+1)(z+1)$

$$= \frac{7z(z+1)(z+2)(z-2)}{4z(z+2)(z+1)(z+1)} = \boxed{\frac{7(z-2)}{4(z+1)}} \quad (A)$$

(69)  $\left(\frac{x+5}{3x+2}\right)\left(\frac{2x-3}{x-5}\right)$   $\leftarrow$  no factors are identical on top AND bottom (nothing cancels) SO FOIL

$$\frac{(x+5)(2x-3)}{(3x+2)(x-5)} = \frac{2x^2 - 3x + 10x - 15}{3x^2 - 15x + 2x - 10}$$

minus

$$= \boxed{\frac{2x^2 + 7x - 15}{3x^2 - 13x - 10}}$$

minus

(D)

sorry...  
Almost "3x-2"  
wrote "3x-2"  
instead which  
messed up some  
signs (2)

(70)  $\frac{x^2 + 8x + 16}{x + 3} \cdot \frac{2x + 8}{x^2 - 9}$

$\frac{(x^2 + 8x + 16)}{(x + 3)}$   
*x, x sign (+) same sign 4, 4*

FLIP AND multiply by reciprocal  
 ← difference of squares  
 NOW FACTOR ALL FOUR POLYNOMIALS

$\frac{(x + 4)(x + 4)}{(x + 3)} \cdot \frac{(x + 3)(x - 3)}{2(x + 4)}$

$= \frac{(x + 4)(x + 4)(x + 3)(x - 3)}{2(x + 3)(x + 4)} = \boxed{\frac{(x + 4)(x - 3)}{2}}$

(71)  $\frac{3x}{5} \cdot \left(\frac{3x}{5}\right) = \left(\frac{3x}{5}\right)$

$\frac{x}{4} + \frac{x}{4} \leftarrow \text{make one fraction w/ common denom} \rightarrow \frac{x}{4} + \frac{2x}{4} = \left(\frac{3x}{4}\right)$

$= \frac{3x}{5} \cdot \frac{3x}{4} = \frac{3x}{5} \cdot \frac{4}{3x} = \frac{12x}{15x} = \boxed{\frac{4}{5}}$   
 FLIP to multiply by reciprocal

(72)  $x = 10\%$  soln amount  
 $y = 15\%$  soln amount

$(x + y = 100 \leftarrow \text{TOTAL soln}) = 100$   
 $.10x + .15y = .12(100) \leftarrow \text{amt of actual saline}$

use elimination  
 $-.10x + .10y = -10$   
 $.10x + .15y = 12$   


---

 $.05y = 2$   
 $y = \frac{2}{.05}$   
 $y = 40 \text{ mL}$   
 $x = 100 - y$   
 $x = 60 \text{ mL}$

(A)

(73) over whole trip, Andy Drove  
 $45 \text{ mph} \cdot 4 \text{ hr} = \boxed{180 \text{ miles}}$

If he Drove  $40 \text{ mph} \cdot 3 \text{ hr} = 120 \text{ miles}$  in  
the first three hours, he must  
have driven  $180 - 120 = 60 \text{ miles}$  in  
the final hour... thus his speed  
was  $\boxed{60 \text{ mph}}$  (B)

(74) 1st pipe has speed:  $\frac{1 \text{ tank}}{20 \text{ min}} = \frac{1}{20} \text{ tank per min}$

2nd pipe has speed:  $\frac{1 \text{ tank}}{30 \text{ min}} = \frac{1}{30} \text{ tank per min}$

So in one minute

together, they fill  $\left(\frac{1}{20} + \frac{1}{30}\right)$  tank per min  
 $= \frac{3}{60} + \frac{2}{60} = \frac{5}{60} = \frac{1}{12} \text{ tank per min}$

thus, to fill the whole tank together  
will take  $\boxed{12 \text{ min}}$

(NOTE A: 60 min, B: 25 min make no  
sense... they can't possibly slow down  
by having more pumps working)

(D)

(75) each hour, they get 650 miles  
(400+250)<sup>(x)</sup> farther apart.

So the distance,  $d$ , between them

$$\text{is } d = 650x$$

$$1625 = 650x$$

$$\frac{1625}{650} = 2.5 = x$$

2.5 hrs

(A)

(76)  $x = \text{Amt pure juice}$

~~0.04~~

$$1x + .10(2) = .25(x+2)$$

↑  
100% of  
 $x$  is  
juice

↑  
only  
10% is  
juice

total  
amt of  
fluid  
25% of whole  
amt is juice

$$x + .2 = .25x + .5$$

$$.75x = .3$$

$$x = .3 / .75 = .4 \quad (A)$$

(77) A FXN MEANS NO repeats in  
 $X$  (DOMAIN)

~~(A) no,  $x = -2$  repeats~~

(B) yes

~~(C) no,  $x = 4$  repeats~~

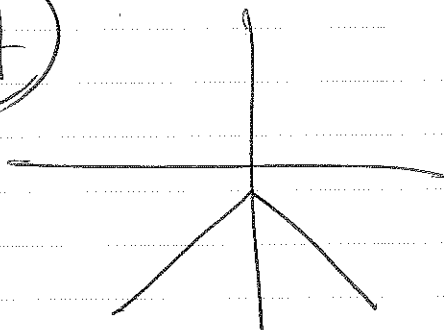
~~(D) no,  $x = 10$  repeats~~

(B)

(78) y-values negative means  
entire graph is below the x-axis  
(so in quadrants III and IV only)

NO	NO
yes	yes

(A)



(79) DOMAIN IS ALL x-values (inputs)

OF f(x) ... SINCE  
the f(x) is just four points

{ (1, -4), (2, -5), (4, -1), (5, -2) }

D: x = 1, 2, 4, 5

{ 1, 2, 4, 5 } (D)

(80) to be a FN graph must pass  
the vertical line test (ANY vertical  
line through the curve intersects at most  
ONCE)

(D) Fails

