

## CALCULATORS ARE NOT PERMITTED.

The format of the exam is identical to the format of this review. Only the actual values in the questions will vary.

**Multiple-Choice:** There will be 20 multiple-choice questions (worth 3 points each.) Only your answer to these questions will receive credit.

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| <p><b>Free-Response:</b> (Total 20 points...exact points are listed in <i>italics</i> in each problem.)<br/>You must show a reasonable amount of work that leads to your answer. Where it is impossible to show work, explain the mental leaps that you made to draw your conclusion. (<i>5 points each</i>)</p> |
| <p><b>Consider the function <math>f(x) = x^2 + 4</math> on <math>[-2, 6]</math>. Approximate the area under the curve on the given interval using each method specified.</b></p>   |
| <p>A. Consider the function <math>f(x) = x^2 + 4</math> on <math>[-2, 6]</math>. Approximate the area under the curve on the given interval using each method specified. <b><u>RRAM with <math>n = 8</math>.</u></b></p>   |
| <p>B. Consider the function <math>f(x) = x^2 + 4</math> on <math>[-2, 6]</math>. Approximate the area under the curve on the given interval using each method specified. <b><u>MRAM with <math>n = 8</math>.</u></b></p>   |
| <p>C. Consider the function <math>f(x) = x^2 + 4</math> on <math>[-2, 6]</math>. Approximate the area under the curve on the given interval using each method specified. <b><u>Trapezoidal Approximation with <math>n = 8</math>.</u></b></p>  |
| <p>D. Consider the function <math>f(x) = x^2 + 4</math> on <math>[-2, 6]</math>. Approximate the area under the curve on the given interval using each method specified. <b><u>Simpson's Method with <math>n = 8</math>.</u></b></p>   |

## Ch.5A Review

For each problem, approximate the area under the curve over the given interval using LRAM with  $n = 4$ .

1)  $y = -x^2 + 11$ ;  $[-1, 3]$

- A)  $\frac{115}{3} \approx 38.333$       B) 38  
C) 40      D) 36

For each problem, approximate the area under the curve over the given interval using RRAM with  $n = 4$ .

2)  $y = x^2 - 2x + 2$ ;  $[-2, 2]$

- A) 10      B)  $\frac{31}{3} \approx 10.333$   
C) 12      D)  $\frac{29}{3} \approx 9.667$

For each problem, approximate the area under the curve over the given interval using 5 trapezoids.

3)  $y = x^2 - 2x + 2$ ;  $[-1, 4]$

- A)  $\frac{107}{6} \approx 17.833$       B) 17  
C)  $\frac{35}{2} = 17.5$       D)  $\frac{39}{2} = 19.5$

Evaluate each sum.

4)  $\sum_{k=1}^n 8k^2$

- A)  $8n^3 + 12n^2 + 4n$   
B)  $\frac{8n^3}{3} + 4n^2 + \frac{4n}{3}$   
C)  $\frac{32n^3}{3} + 16n^2 + \frac{16n}{3}$   
D)  $\frac{8n^3}{9} + \frac{4n^2}{3} + \frac{4n}{9}$

5)  $\sum_{k=1}^n (2k^2 + 3)$

- A)  $\frac{2n^3}{9} + \frac{n^2}{3} + \frac{10n}{9}$   
B)  $\frac{n^3}{3} + \frac{n^2}{2} + \frac{5n}{3}$   
C)  $\frac{2n^3}{3} + n^2 + \frac{10n}{3}$   
D)  $\frac{4n^3}{3} + 2n^2 + \frac{20n}{3}$

For each problem, use a left-hand Riemann sum to approximate the integral based off of the values in the table.

6)  $\int_0^9 f(x) dx$

|        |   |   |   |   |   |
|--------|---|---|---|---|---|
| $x$    | 0 | 5 | 6 | 7 | 9 |
| $f(x)$ | 6 | 5 | 3 | 5 | 4 |

- A) 38      B) 48  
C) 53      D) 49

For each problem, use a right-hand Riemann sum to approximate the integral based off of the values in the table.

7)  $\int_0^{10} f(x) dx$

|        |   |   |   |   |    |
|--------|---|---|---|---|----|
| $x$    | 0 | 5 | 7 | 9 | 10 |
| $f(x)$ | 8 | 6 | 8 | 7 | 6  |

- A) 59      B) 72  
C) 70      D) 66

Evaluate each definite integral.

8)  $\int_0^4 (-2x + 2) dx$

- A) -12      B) -14  
C) -16      D) -8

9)  $\int_{-7}^{-3} (x + 2) dx$

- A) -18      B) -12  
C) -19      D) -13

10)  $\int_{-4}^{-2} \frac{4}{x} dx$

- A)  $5 \ln 2 \approx 3.466$   
B)  $4 \ln 2 - 4 \ln 4 \approx -2.773$   
C)  $12 \ln 2 - 7 \ln 4 \approx -1.386$   
D)  $4 \ln 11 - 2 \ln 4 \approx 6.819$

11)  $\int_{-1}^2 -5x^{\frac{1}{3}} dx$

- A)  $\frac{-20\sqrt[3]{2} + 17}{5} \approx -1.64$   
B)  $\frac{-30\sqrt[3]{2} + 15}{4} \approx -5.699$   
C)  $\frac{-30\sqrt[3]{2} + 13}{9} \approx -2.755$   
D)  $\frac{33\sqrt[3]{7} - 15}{4} \approx 12.032$

Evaluate each indefinite integral.

12)  $\int 4 dx$

- A)  $4 + C$       B)  $C$   
C)  $4x + C$       D)  $-3x + C$

$$13) \int \frac{-5x^2 - 4}{x^2} dx$$

- A)  $-5x - \frac{4}{x} + C$   
 B)  $-5x + \frac{4}{x} + C$   
 C)  $-5 + \frac{4}{x^2} + C$   
 D)  $-9x + C$

$$14) \int \frac{6(-5x^{10} + 2)}{x^5} dx$$

- A)  $-5x^5 - \frac{3}{x^5} + C$   
 B)  $-18x + C$   
 C)  $-5x^6 - \frac{3}{x^4} + C$   
 D)  $-30x^6 + \frac{12}{x^4} + C$

$$15) \int x^2(-20x^2 - 12x - 9) dx$$

- A)  $-41x + C$   
 B)  $-4x^4 - 3x^3 - 3x^2 + C$   
 C)  $-4x^5 - 3x^4 - 3x^3 + C$   
 D)  $-20x^5 - 12x^4 - 9x^3 + C$

$$16) \int \frac{-32x^3 x^{\frac{3}{5}} + 75x^3 x^{\frac{1}{4}} - 200}{20x^3} dx$$

- A)  $-x^{\frac{3}{5}} + 3x^{\frac{1}{4}} + \frac{5}{x^3} + C$   
 B)  $-\frac{157x}{20} + C$   
 C)  $-x^{\frac{8}{5}} + 3x^{\frac{5}{4}} + \frac{5}{x^2} + C$   
 D)  $-\frac{8x^{\frac{8}{5}}}{5} + \frac{15x^{\frac{5}{4}}}{4} - \frac{10}{x^2} + C$

$$17) \int -3 \cdot \csc^2 x dx$$

- A)  $3\sin x + C$       B)  $3\cos x + C$   
 C)  $3\cot x + C$       D)  $3\tan x + C$

$$18) \int -2 \cdot \sec^2 x dx$$

- A)  $-2\sec x + C$   
 B)  $-2\tan x + C$   
 C)  $-2\cos x + C$   
 D)  $-2\cot x + C$

$$19) \int -4\sin x dx$$

- A)  $4\cot x + C$       B)  $4\cos x + C$   
 C)  $4\sec x + C$       D)  $4\csc x + C$

$$20) \int e^x dx$$

- A)  $e^x + C$       B)  $2e^x + C$   
 C)  $4^x + C$       D)  $\frac{4^x}{\ln 4} + C$

## Answers to Ch.5A Review

1) B  
5) C  
9) B  
13) B  
17) C

2) A  
6) B  
10) B  
14) C  
18) B

3) C  
7) D  
11) B  
15) C  
19) B

4) B  
8) D  
12) C  
16) C  
20) A